



Determination of Young's Modulus of Aluminium, Copper, Iron, Brass and Steel Alloys by Using Double Exposure Holographic Interferometry (Dehi) Technique

H. R. KULKARNI^{1*}, S. N. SHUKLA² and M. B. DONGARE³

¹KJEI's KJ College of Engineering and Management Research, Pune, Maharashtra, India.

²Matoshri College of Engineering and Research Center, Eklahare Nasik, Maharashtra, India.

³Ex-Professor, Department of Physics, Shivaji University Kolhapur, Maharashtra, India.

Abstract

Double Exposure Holographic Interferometry(DEHI) technique has wide applications in the field of science and engineering. DEHI can be used to determine very small surface changes in an object at very small interval of time. In present case, DEHI technique is used to record the hologram of the same object at different times subjected to different loads. This method has been advantageously used to determine Young's Modulus (Y) of Aluminium, Copper, iron, brass and some steel alloys. It is found that the values of Y obtained by using DEHI technique are in close agreement with standard values of Y available for respective metals and their alloys. The method is also used to make standard relation between effect of carbon composition and Y of steel alloys.



Article History

Received: 22 September 2017

Accepted: 04 October 2017

Keywords:

DEHI, Double Exposure Holographic Interferometry, Young's Modulus.

Introduction

DEHI technique is used to record the holograms of same objects at different times¹. This method has some advantages over other techniques particularly for studying transient phenomenon. The analysis is, of course, not significantly different from analysis given for single exposure technique and the resulting interference pattern is determined by the phase difference between the object wave in first position and object wave in second position². This

technique can be used in the study of stress-strain relation, and fluid mechanics³, fracture mechanics for non-destructive testing⁴. Hologram interferometry can also be used to show changes of shape in a specimen⁵.

The qualitative determination of mechanical strain⁶ on surface of arbitrary shaped object through holographic interferometry requires the solution of following three basic problems.

CONTACT H. R. Kulkarni ✉ hrkulkarni@rediffmail.com 📍 KJEI's KJ College of Engineering and Management Research, Pune, Maharashtra, India.

© 2017 The Author(s). Published by Oriental Scientific Publishing Company.

This is an Open Access article licensed under a Creative Commons Attribution-NonCommercial-ShareAlike 4.0 International License (<https://creativecommons.org/licenses/by-nc-sa/4.0/>), which permits unrestricted NonCommercial use, distribution, and reproduction in any medium, provided the original work is properly cited.

To link to this Article: <http://dx.doi.org/10.13005/msri/140207>

- i. Relation between surface strain and surface displacement;
- ii. Relation between derivation of the surface displacement and the interference fringes in the image plane;
- iii. Interpolation of interference fringe pattern and quantitative determination of interference phase.

equation of cantilever is given by,

$$\Delta Z = (WL^3) / (3YI) \quad \text{.....(1)}$$

Where,

W = load applied in kg

L = effective span in cm

Y = Young's modulus in kgF / cm²

I = moment of inertia in cm⁴, can be obtained from physical dimensions of cantilever. Its value for rectangular beam of width 'a' and thickness 'b' is $ab^3 / 12$.

Equation (1) can be written as,

$$Y = (WL^3) / (3I \Delta Z) \quad \text{.....(2)}$$

Where ΔZ is measured from holographic interferometry.

Let θ_i and θ_o be the angle defining the directions of illumination and observation respectively. These are measured from the geometry of figure as shown in Figure 2. The path difference Δ between two rays scattered from the two identical points on the object is given by,

$$\Delta = \Delta Z \cdot n \cdot (\cos\theta_i + \cos\theta_o) \quad \text{.....(3)}$$

Where, n = refractive index, usually 1 for air.

If there are N fringes produced up to the span length L of the cantilever counted from the fixed end, then,

$$\Delta Z = N\lambda / (\cos\theta_i + \cos\theta_o) \quad \text{.....(4)}$$

Substituting the value of ΔZ in equation 2. Then the value of Young's modulus can be calculated from,

$$Y = WL^3 (\cos\theta_i + \cos\theta_o) / (3I N\lambda) \quad \text{.....(5)}$$

Experimental Results of Y for Metals and Alloys

Young's modulus has been determined for aluminium, copper, iron, brass and certain steel alloys by using DEHI technique. The samples for this purpose were obtained from Mayura Steel Industries, Kolhapur. The

The development of practical technique for obtaining quantitative information⁷ from double- exposure hologram is still one of the most interesting problems in holographic interferometry. The applications of holographic interferometry techniques to non-destructive testing have received a great deal of attention in recent years. Because of its extreme sensitivity, holographic interferometry allows for the detection of small defects and anomalies in diffuse three dimensional objects⁷⁻⁹. Various holographic methods are described¹⁰⁻¹² to measure 3-D displacements of object under loading. These include viewing of surface of object through different points of hologram through various angles and counting the number of fringes that pass through the point under consideration between the two exposures is very small or less than one fringe. The success of holographic non-destructive testing¹³ of a material, however, depends upon the stressing technique adopted. The stressing should deform the body under test in such a manner that the 'good' areas are distinguished from the 'bad' areas simply by studying the interference generated on the holographic interferogram.

Measurement of Young's Modulus¹⁴

Young's modulus of material can be calculated using deflection equation of cantilever. The deflection

Table 1: Constituents of steel alloys

Constit- uents %	Steel samples		
	K ₁	K ₂	K ₃
C	0.184	0.40	1.17
Mn	0.93	0.090	13.15
Si	0.41	0.42	0.42
S	0.037	0.039	0.004
P	0.030	0.038	0.066
Cr	0.099	0.763	0.23
Ni	---	3.258	0.038
Mo	30.00	0.231	---

constitution of alloy and their composition as well as their dimensions are given in Table 1.

The experimental arrangement for recording double exposure hologram with loaded objects is as shown in Figure 1.

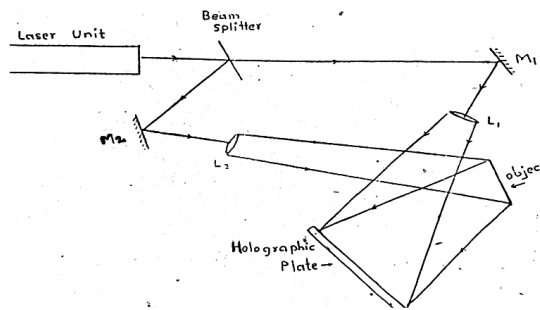


Fig. 1 : Experimental arrangement for DEHI

Double exposure holograms of the corresponding objects were recorded at two different situations. One at its normal state and other at deformed state due to application of load. For the application of load, string and pulley arrangement was used as shown in Figure 3.

The holograms were recorded on 8E75HD holographic plate using He-Ne laser of 2mw. The two beam off axis method was used to record the holograms. The holograms were processed in usual manner. The reconstructed holograms revealed

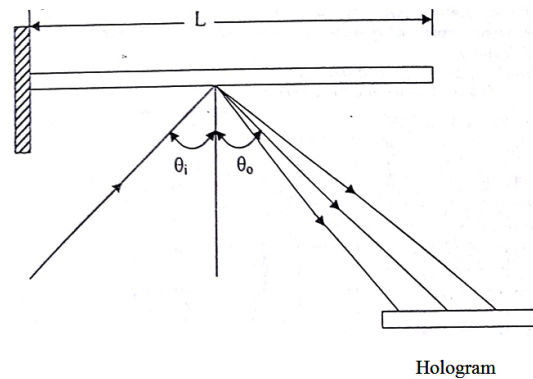


Fig. 2: Measurement of angles

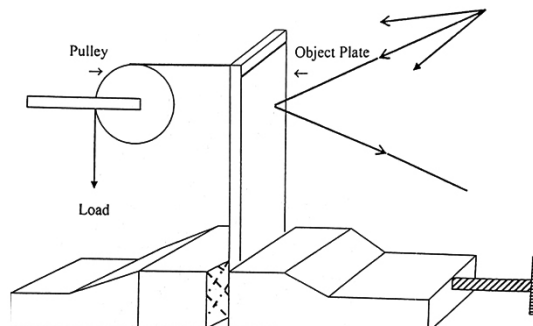


Fig. 3: Object when load is applied

number of fringes located on the surface of metal plates. The exposure time of 7sec each was given to both the exposures. The object dimensions have been accurately measured and presented in Table 2. The number of fringes were accurately counted.

Table 2: Determined values of Y

Object Plate	Length L in cm	Breadth 'a' in cm	Depth 'b' in cm	Load applied W in kg	No of fringes located on the object	Angle of (in degrees)		Young's Modulus Y in kgF / cm ²	
						Illumi-nation	Scatt-ering	Determined values	Standard Values
						θ_i	θ_o		
Al	3	3	0.11	0.007	10	6° 30'	46°	0.672 x 106	0.70 x 106
Cu	1.8	3	0.11	0.65	11	6° 00'	44° 30'	1.240 x 106	1.240 x 106
Iron	3	3	0.12	0.14	36	5° 30'	48°	2.130 x 106	2.00 x 106
Brass	3	3	0.011	0.015	15	6° 30'	44° 30'	0.970 x 106	0.90 to 1 x 106
K1	2.4	3	0.38	3	12	4° 30'	48°	2.230 x 106	-----
K2	2.4	2.9	0.353	3	15	7° 00'	46°	2.311 x 106	-----
K3	2.5	3	0.31	1.8	13	4° 30'	48°	2.549 x 106	-----

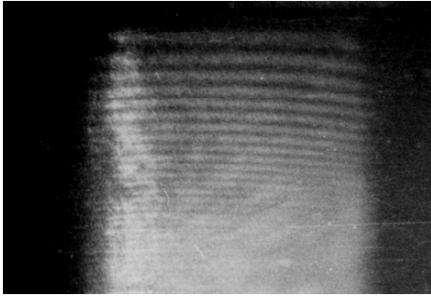


Photo 1: Mechanically stressed Al plate

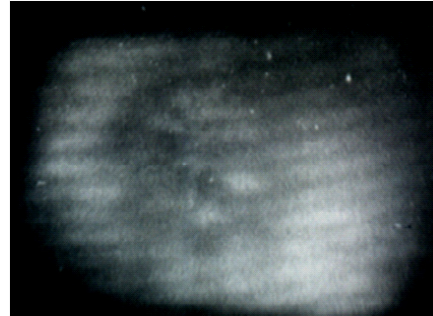


Photo 5: Mechanically stressed K1 plate

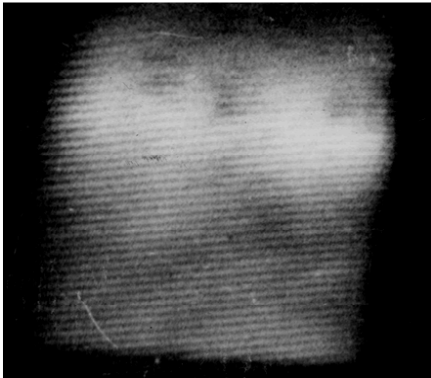


Photo 2: Mechanically stressed Cu plate

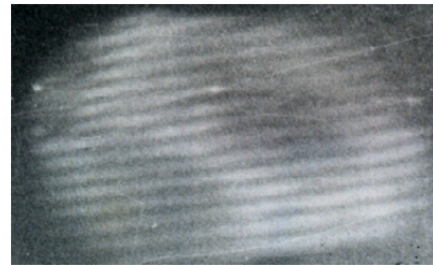


Photo 6: Mechanically stressed K2 plate

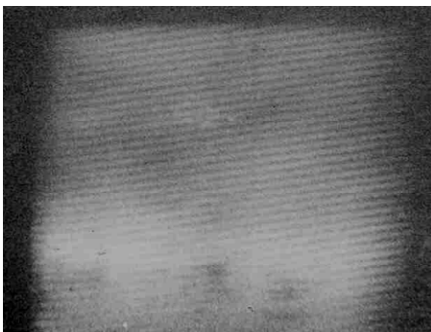


Photo 3: Mechanically stressed iron plate

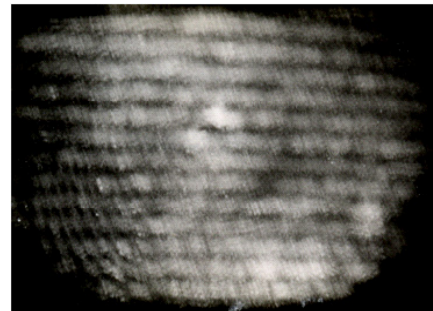


Photo 7: Mechanically stressed K3 plate



Photo 4: Mechanically stressed brass plate

These are shown in Photographs 1-7. Making the use of Equation (5), Young's modulus of material of object has been determined. The values of Y calculated by this method have been entered in Table 2 along with object dimensions and angle of illumination and scattering of light from the object surface.

Results and Discussion

With the help of DEHI technique, the calculated values of Y for Aluminium, Copper, brass, iron and steel alloys plates are given in Table 2. It is found that

the values of Y calculated are in close agreement with the standard values.

In case of steel alloys K_1 , K_2 and K_3 (general titles given) value of Y found is higher than that of iron. It is mostly dependent of percentage of carbon in that alloy. This percentage of carbon is given in Table 1. The carbon content of K_1 , K_2 , and K_3 is in the increasing order resulting to increase in their Young's modulus. For sample K_1 , it is 1.04 times greater than that of iron and K_2 it is observed 1.08

times greater while for K_3 1.19 time greater that of iron. The values determined for samples K_1 , K_2 , and K_3 are not available anywhere. The values of Y determined for Aluminium, Copper, brass, and iron are in close agreement with the available standard values. These results indicate DEHI technique can be used to determine the standard values of Young's modulus of elastic material. This result confirms that the values of Y determined for samples K_1 , K_2 , and K_3 are correct.

References

1. Helfinger, L. O. Brooks, R. E. and Wuerker, R. F.; *J. Appl. Phys.*, 37, 642 (1966).
2. L. H. Tanner, *J. Sci. Instrum.*, 44, 1015 (1967).
3. T. D. Dudderar; *Exp. Mech.*, 9, 281 (1969).
4. W. H. Steel; *Interferometry*, Cambridge University Press, page 188 (1968).
5. R. Dandliker, B. Eliasson, B. Ineichen, F. M. Motterer; *The engineering use of Coherent Optics*, Cambridge University Press, Cambridge, page 99-117 (1976).
6. E. Marom, A. A. Friesem, E. Wiener; *Avnear, Applications of Holography and Optical data processing*, Pergamon Press, London, page 225 (1977).
7. Robertson, E. R.; *The Engineering Uses of Coherent Optics*, Cambridge University Press (1976).
8. Erf, R. K.; *Holographic Non-destructive Testing*, Academic Press, New York (1974).
9. P. Hariharan; *Optical Holography, Principles, Techniques and Applications*, Cambridge University Press, page 214 (1984).
10. P. W. King III; *Appl. Opt.*, 13, 231 (1974).
11. B. D. Hansche, G. G. Murphy; *Appl. Opt.*, 13, 630 (1974).
12. A. V. S. S. R. Sarma, T. G. George Kutty; *Appl. Opt.*, 17, 3964 (1978).
13. P. C. Mehta, D. Mohan, C. Bhan, P. Lal, R. Rhidaynath; *Optics and Laser Technology*, 269 (1982).
14. R. S. Sirohi; *A Course of Experiments with He-Ne laser*, Wiley Eastern Limited, New Delhi, Page 67 (1986).